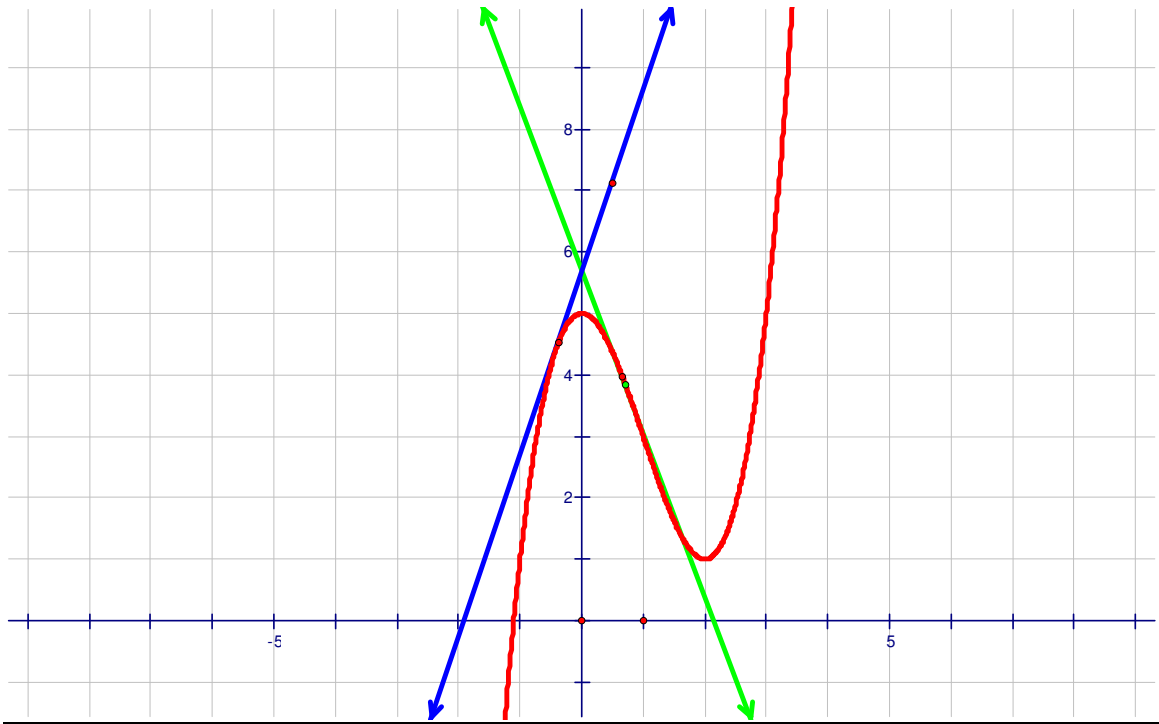


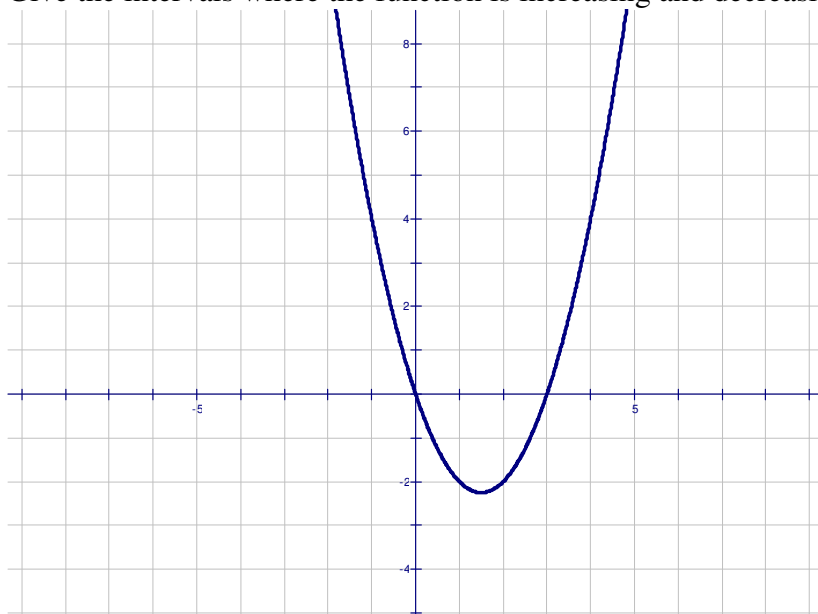
Section 10.1 A

Increasing and Decreasing Functions



Example 1

Give the intervals where the function is increasing and decreasing.

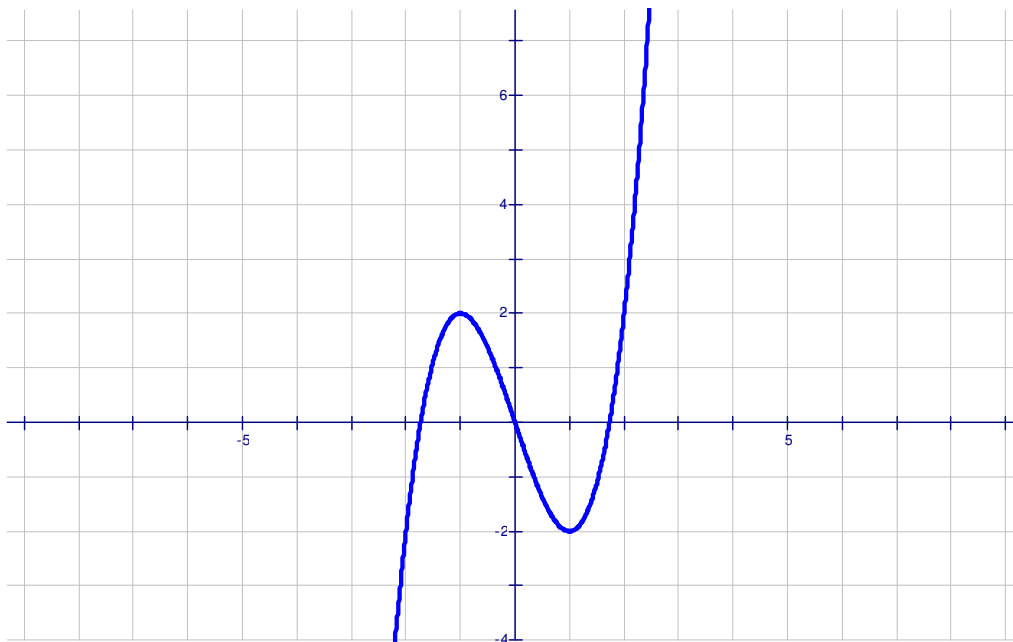


Decreasing: $\left(-\infty, \frac{3}{2}\right)$

Increasing: $\left(\frac{3}{2}, \infty\right)$

Example 2

Give the intervals where the function increasing and decreasing



Increasing: $(-\infty, -1) \cup (1, \infty)$ Decreasing: $(-1, 1)$

Test for increasing and decreasing functions

Let f be a differentiable function on the interval

- 1) If $f'(x) > 0$ for all x in (a, b) , then f is increasing on (a, b)
 - 2) If $f'(x) < 0$ for all x in (a, b) , then f is decreasing on (a, b)
 - 3) If $f'(x) = 0$ for all x in (a, b) , then f is constant on (a, b)
-

Example 3

Give the intervals where the function is increasing and decreasing

$$f(x) = x^2 - 4x$$

$$f'(x) = 2x - 4$$

$$2x - 4 = 0$$

$$2x - 4 + 4 = 0 + 4$$

$$2x = 4$$

$$\frac{2x}{2} = \frac{4}{2}$$

$$x = 2$$

$$f'(-1) = 2(-1) - 4 = -2 - 4 = -6$$

$$f'(3) = 2(3) - 4 = 2$$

Interval	$(-\infty, 2)$	$(2, \infty)$
Test Value	$x = -1$	$x = 3$
Sign of $f'(x)$	Negative	Positive
Conclusion	Decreasing	Increasing

Example 4

Find the intervals where the function is decreasing and increasing

$$f(x) = x^3 - 4$$

$$f'(x) = 3x^2$$

$$3x^2 = 0$$

$$\frac{3x^2}{3} = \frac{0}{3}$$

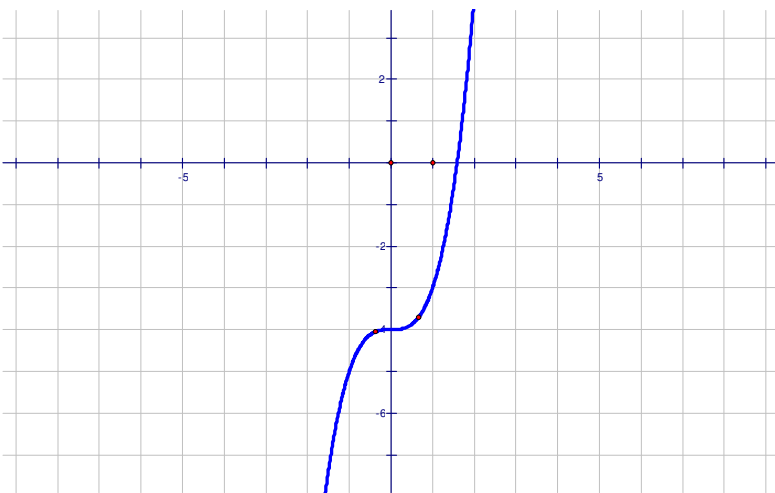
$$x^2 = 0$$

$$x = 0$$

$$f'(-1) = 3(-1)^2 = 3$$

$$f'(1) = 3(1)^2 = 3$$

Interval	$(-\infty, 0)$	$(0, \infty)$
Test Value	$x = -1$	$x = 1$
Sign of $f'(x)$	Positive	Positive
Conclusion	Increasing	Increasing



Example 5

Find the intervals where the function is increasing or decreasing: $f(x) = x^3 - 3x^2$

$$f'(x) = 3x^2 - 6x$$

$$3x^2 - 6x = 0$$

$$3x(x - 2) = 0$$

$$3x = 0 \text{ or } x - 2 = 0$$

$$\frac{3x}{3} = \frac{0}{3} \text{ or } x - 2 + 2 = 0 + 2$$

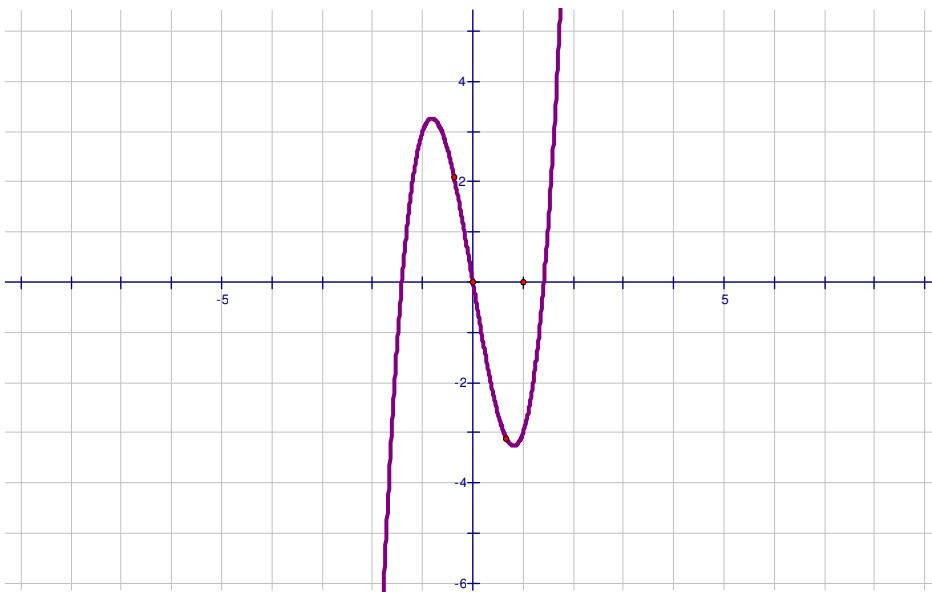
$$x = 0 \qquad x = 2$$

$$f'(-1) = 3(-1)^2 - 6(-1) = 3 + 6 = 9$$

$$f'(1) = 3(1)^2 - 6(1) = 3 - 6 = -3$$

$$f'(3) = 3(3)^2 - 6(3) = 27 - 18 = 9$$

Interval	$(-\infty, 0)$	$(0, 2)$	$(2, \infty)$
Test Value	$x = -1$	$x = 1$	$x = 3$
Sign of $f'(x)$	Positive	Negative	Positive
Conclusion	Increasing	Decreasing	Increasing



Example 6

Find the intervals where the functions is increasing and decreasing

$$f(x) = x^2 - 4$$

$$f'(x) = 2x$$

$$2x = 0$$

$$\frac{2x}{2} = \frac{0}{2}$$

$$x = 0$$

$$f'(-1) = 2(-1) = -2$$

$$f'(1) = 2(1) = 2$$

Interval	$(-\infty, 0)$	$(0, \infty)$
Test Value	$x = -1$	$x = 1$
Sign of $f'(x)$	Negative	Positive
Conclusion	Decreasing	Increasing

Exercises 10.1 A

Find the intervals where the functions is increasing and decreasing.

1) $f(x) = -x^2 - 2x$

2) $f(x) = x^3 + 3$

3) $f(x) = x^2 - 6x + 5$

4) $f(x) = x^3 - 6x^2$

5) $f(x) = -2x^4$

6) $f(x) = x^3 - x$